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Design de structures présentant des diagrammes de rayonnement thermique contrôlés

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1- Motivation initiale

Dans le domaine des **composants photoniques**,
*les phénomènes de **transfert thermique** sont devenus omniprésents:*

- des sources de plus en plus puissantes
- des volumes de plus en plus confinés



Hautes densités d'énergie électromagnétique \Rightarrow Températures élevées



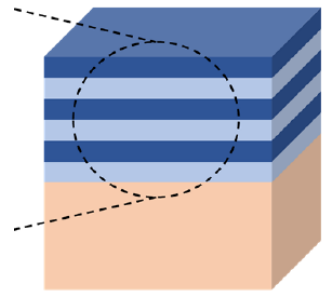
Dérive/dégradation/endommagement



Modélisation de la température photo-induite



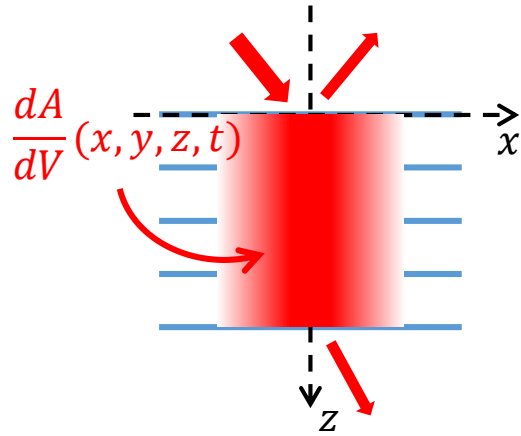
Rayonnement thermique photo-induit: difficulté ou opportunité?



2- Modélisation de la température photo-induite en régime spatio-temporel

A combien ça monte, à quelle vitesse, quand est-ce que ça casse, qu'est-ce qui chauffe?

- Z. M. Zhang, Nano/Microscale Heat Transfer, 2nd ed., Mechanical Engineering Series (Springer International Publishing, 2020)
- M. Mansuripur, G. A. N. Connell, and J. W. Goodman, "Laser-induced local heating of multilayers," Appl. Opt. **21**, 1106–1114 (1982)
- B. Wang, X. Wang, Y. Qin, X. Ni, Z. Shen, and J. Lu, "Temperature field analysis of optical coatings induced by millisecond and nanosecond lasers," Optica Applicata **42**, 783–793 (2012).



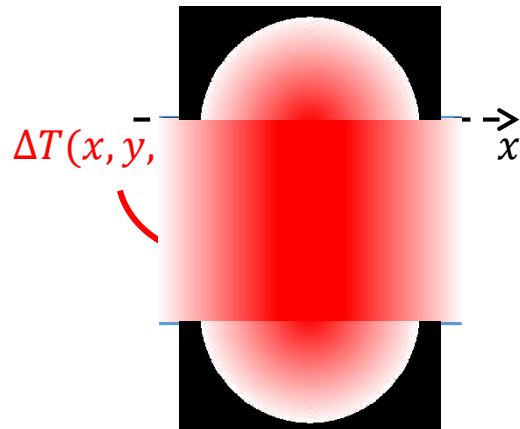
The incident field creates a **4D absorption density** within the stack

$$\frac{dA}{dz}(x, y, z, t)$$



Heat equation: $\Delta T_i(\vec{\rho}, t) - \frac{1}{a_i} \frac{\partial T_i}{\partial t}(\vec{\rho}, t) = -\frac{1}{b_i} S_i(\vec{\rho}, t)$

Heat source created by
absorption



This absorption density is responsible
for a temperature distribution $T(x, y, z, t)$

The heat source in a spatio-temporal regime

Source term = volume density of losses

$$\text{Maxwell equations} \Rightarrow \mathbf{S}_i(\vec{r}, \mathbf{z}, t) = \frac{\partial W_i}{\partial t} = \vec{E}_i \cdot \frac{\partial}{\partial t} (\epsilon_i *_t \vec{E}_i) + \vec{H}_i \cdot \frac{\partial}{\partial t} (\mu_i *_t \vec{H}_i)$$

Collimated and quasi-monochromatic source

$$E_0^+(\vec{r}, z, t) = \mathbf{g}(\vec{r}, \mathbf{z}, t) \cos(2\pi(f_0 t - \vec{v}_0 \cdot \vec{r}))$$



$$\mathbf{S}_i(\vec{r}, \mathbf{z}, t) = \frac{\partial A_i}{\partial z}(\vec{v}_0, z, f_0) \mathbf{g}^2(\vec{r}, z, t)$$

Spatio-temporal envelope

Monochromatic absorption

$$\frac{dA}{dz}(x, y, z, t) \sim \frac{\omega}{2} (\epsilon'' |E|^2 + \mu'' |H|^2)$$

Solving the heat equation

Use an optics/thermal analogy !

Heat diffusion is similar to optical propagation in (specific) metallic media

Second Fourier plane:

$$T(\vec{r}, z, t) \rightarrow \tilde{T}(\vec{r}, z, \Omega) \rightarrow \hat{T}(\vec{v}, z, \Omega)$$

Temporal frequency

Spatial frequency

$$k = \omega \sqrt{\varepsilon(\omega) \mu(\omega)}$$

Optics: $\frac{\partial^2 \vec{E}_i}{\partial z^2}(\vec{v}, z, f) + \alpha_{i,op}^2(\vec{v}, f) \vec{E}_i(\vec{v}, z, f) = \vec{S}_i^E(\vec{v}, z, f)$

Température \Leftrightarrow *champ électrique (TE)*

Thermal: $\frac{\partial^2 \hat{T}_i}{\partial z^2}(\vec{v}, z, f) + \alpha_{i,th}^2(\vec{v}, f) \hat{T}_i(\vec{v}, z, f) = -\frac{1}{b_i} \hat{S}_i(\vec{v}, z, f)$

Flux de chaleur \Leftrightarrow *champ magnétique*

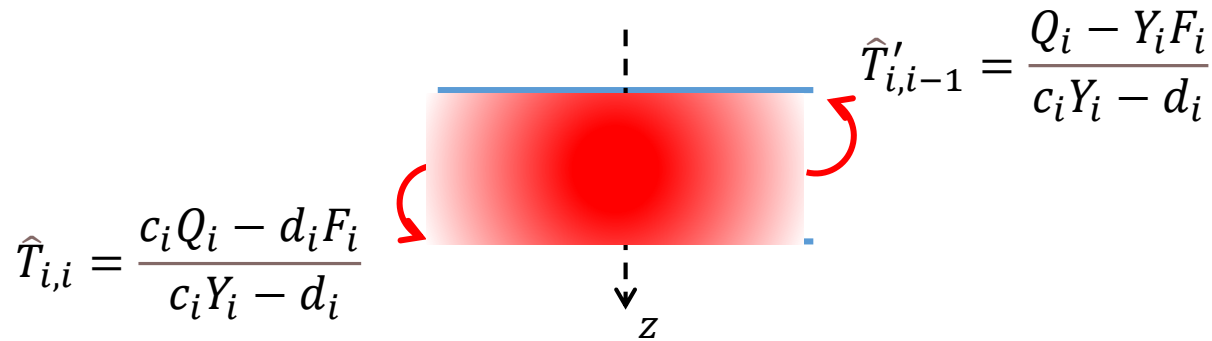
$$k = (1 + j) \sqrt{\frac{\Omega}{2a}}$$

All optical formulae with admittances and effective indices can be used

$$\frac{\partial^2 \hat{T}_i}{\partial z^2}(\vec{v}, z, f) + \alpha_{i,th}^2(\vec{v}, f) \hat{T}_i(\vec{v}, z, f) = -\frac{1}{b_i} \hat{S}_i(\vec{v}, z, f)$$

The heat equation is reduced to an incoherent bulk scattering problem

Each layer is a heat source

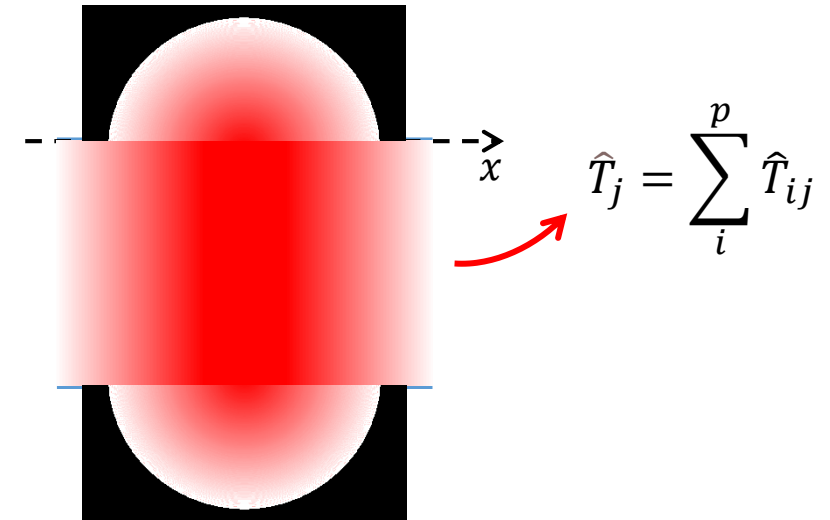


$$\hat{T}_{i,i} = \frac{c_i Q_i - d_i F_i}{c_i Y_i - d_i}$$

$$\hat{T}'_{i,i-1} = \frac{Q_i - Y_i F_i}{c_i Y_i - d_i}$$

The Tp at one surface is created

by all heat sources



$$\hat{T}_j = \sum_i^p \hat{T}_{ij}$$

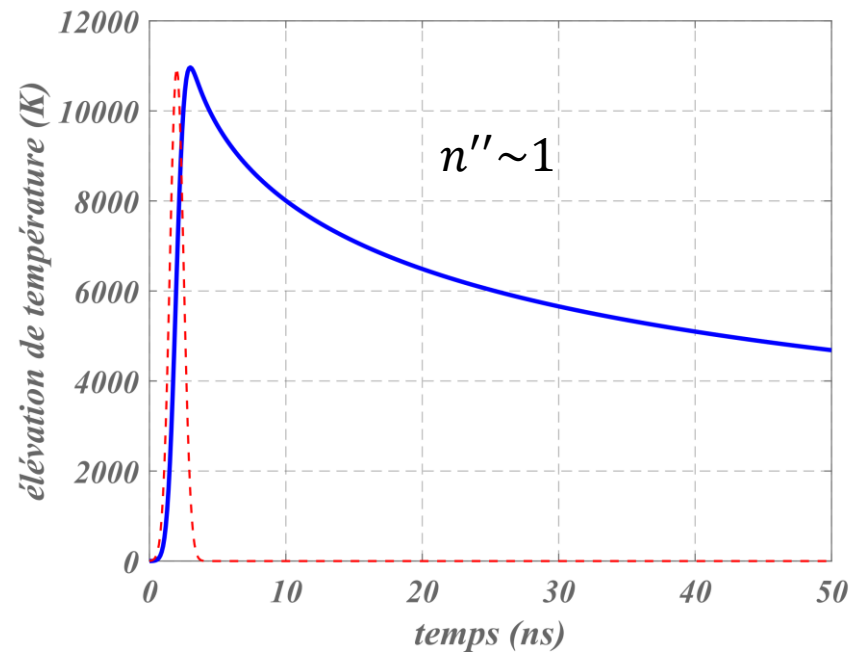
Heat sources do not interfere but the coating design impacts the temperature distribution

Numerical calculation: order of magnitude versus absorption

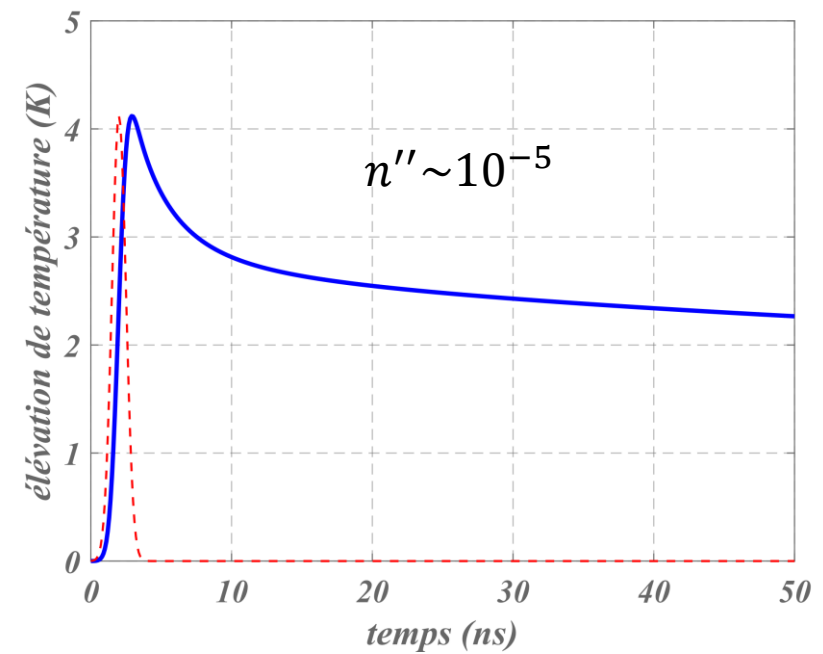
Metallic versus dielectric mirror @ 1064 nm

$$W = 1mJ, \Delta t = 1ns, r = 100\mu m$$

Metallic mirror (prohibitive T_p)



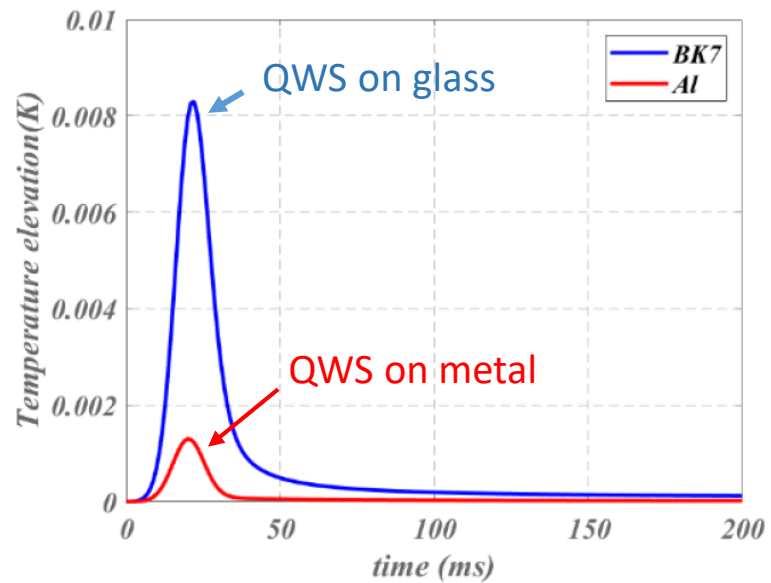
Multidielectric mirror (5K)



T_p difference \Leftrightarrow absorption values (dielectrics versus metals)

But absorption is not the only key: influence of thermal parameters

Comparison of 2 dielectric mirrors on different substrates (metal and glass)



Light does not see the mirror substrate (same absorption)...

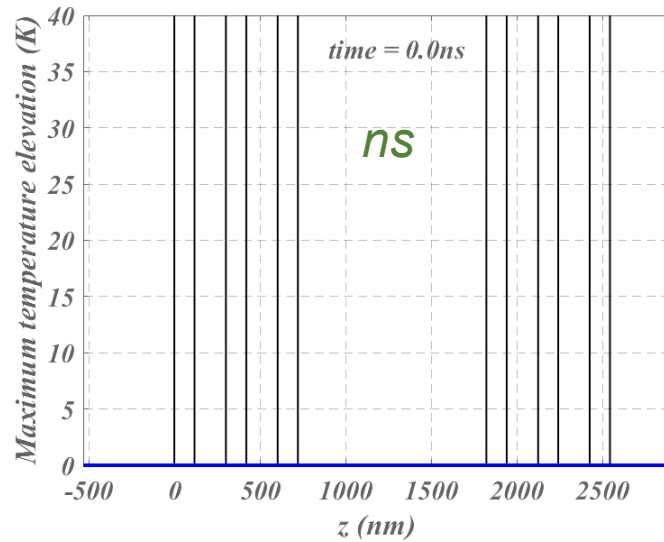
... but the T_p can see the thermal parameters of substrate (heat diffusion)

Tp resolution versus pulse duration

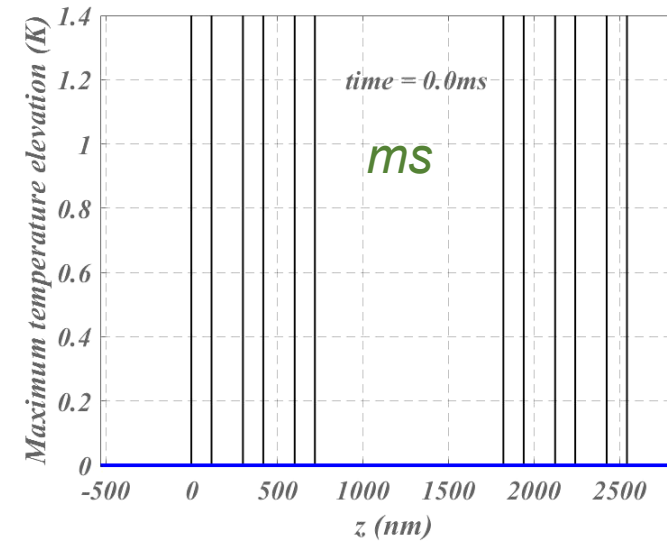
Fabry-Perot filter @ 1064 nm on glass, $n'' = 10^{-5}$

$$W = 1mJ, r = 100\mu m$$

$$\Delta T_{max}(ns) = 40K$$



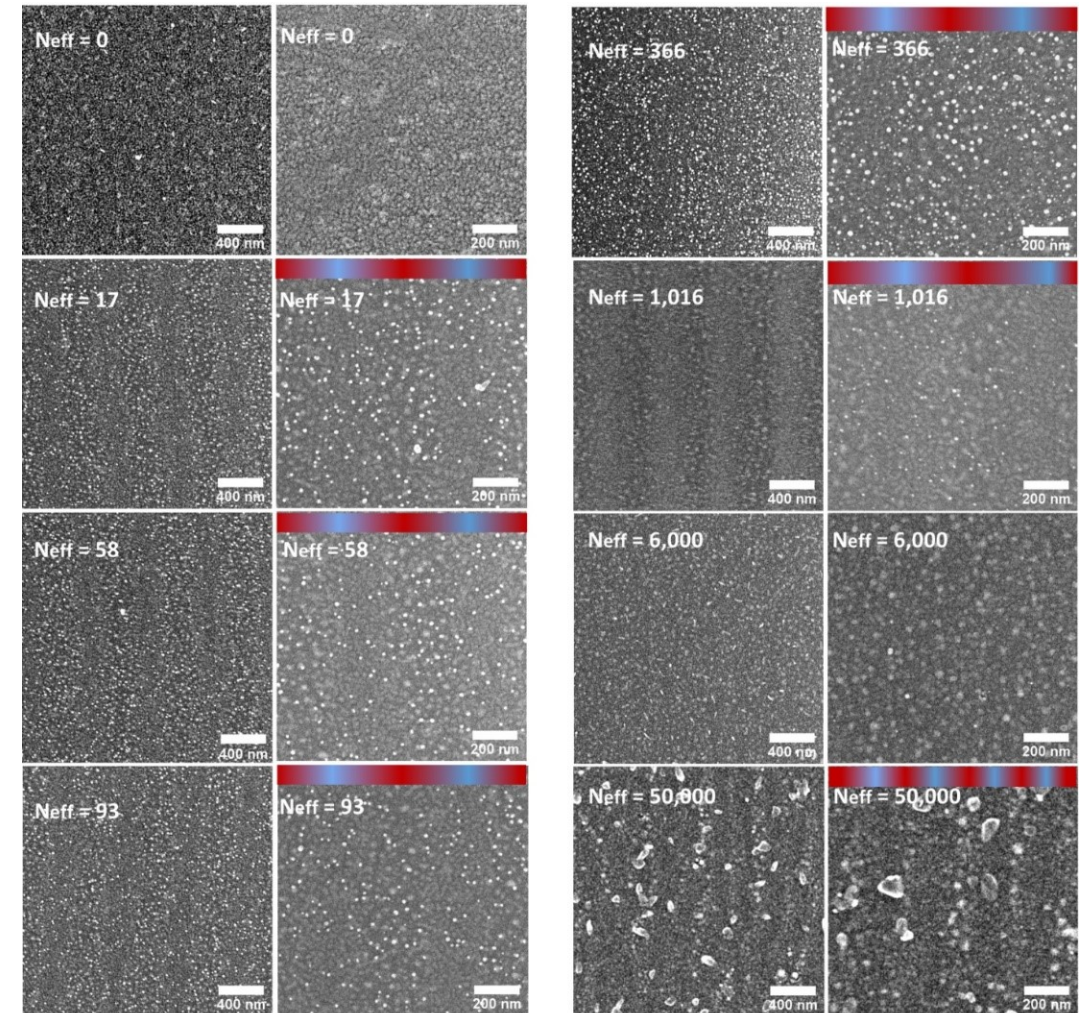
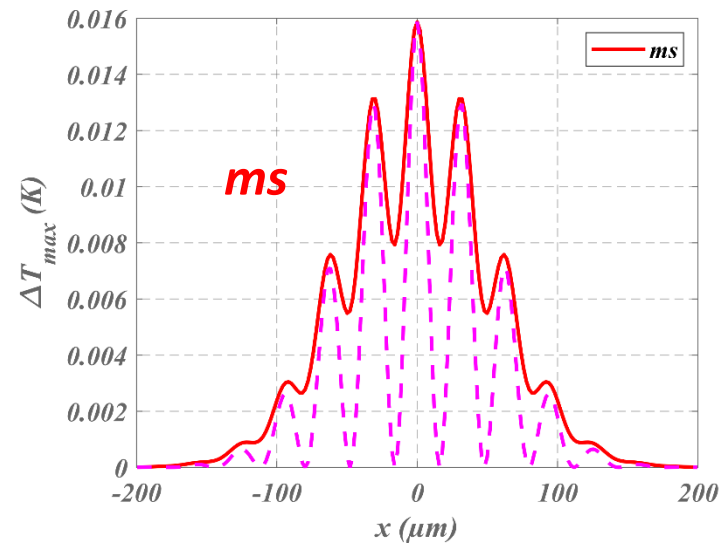
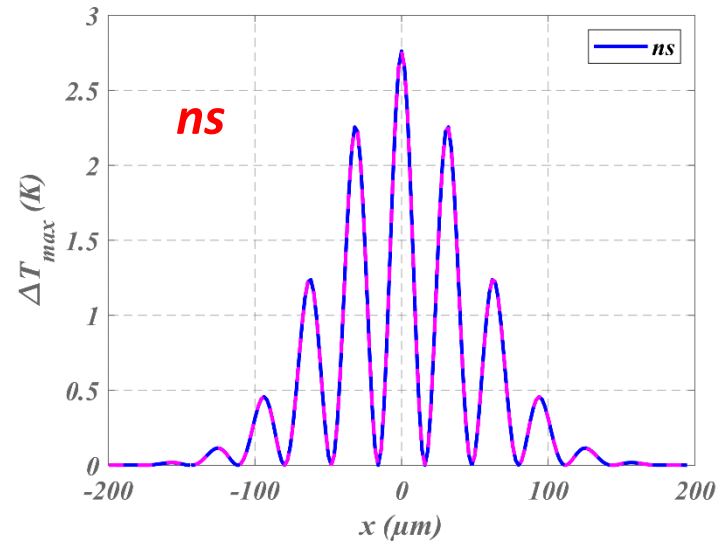
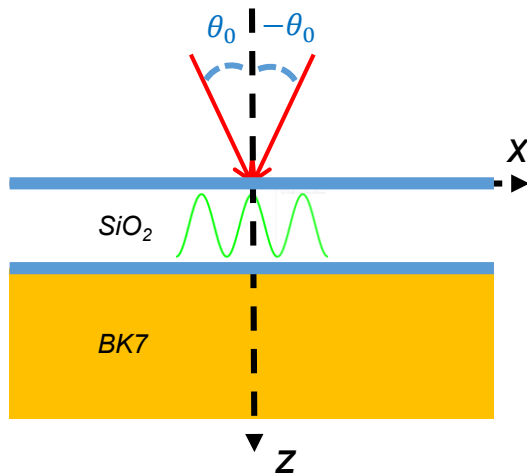
$$\Delta T_{max}(ms) = 1,4K$$



At short pulses (1ns), the temperature follows the stationary electromagnetic field

Optical fringes may create « thermal fringes »

2 beams interference



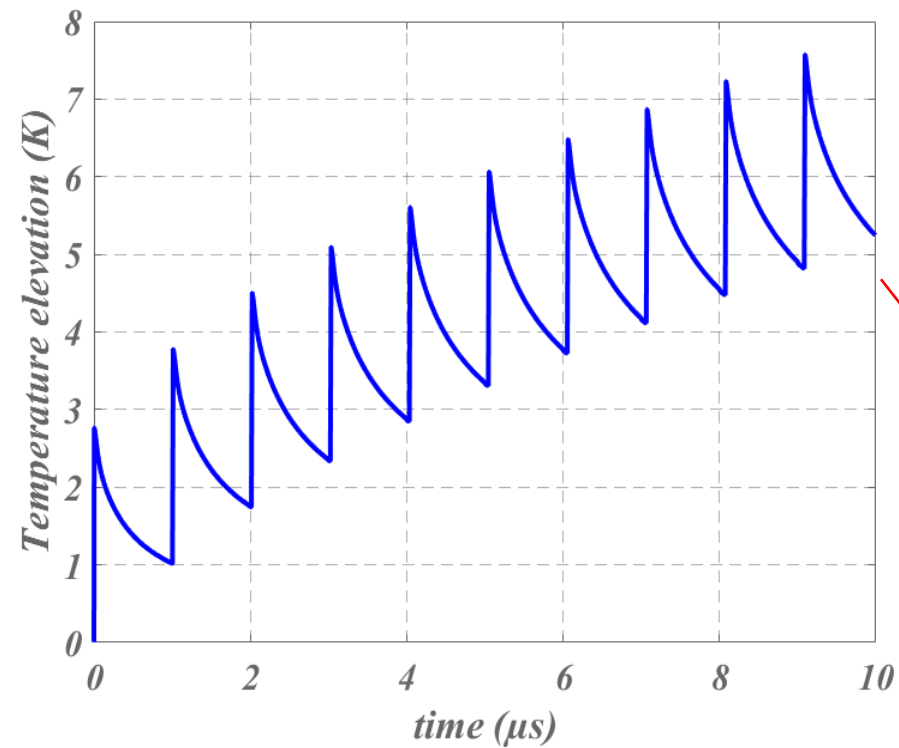
Eles, Balint, Rouquette, Paul, Siegel, Jan, Amra, Claude, Lumeau, Julien, Moreau, Antonin, Hubert, Christophe, Zerrad, Myriam and Destouches, Nathalie.
 "Mechanisms driving self-organization phenomena in random plasmonic metasurfaces under multipulse femtosecond laser exposure: a multitime scale study" *Nanophotonics*, vol. , no. , 2022

Influence of repetition rate

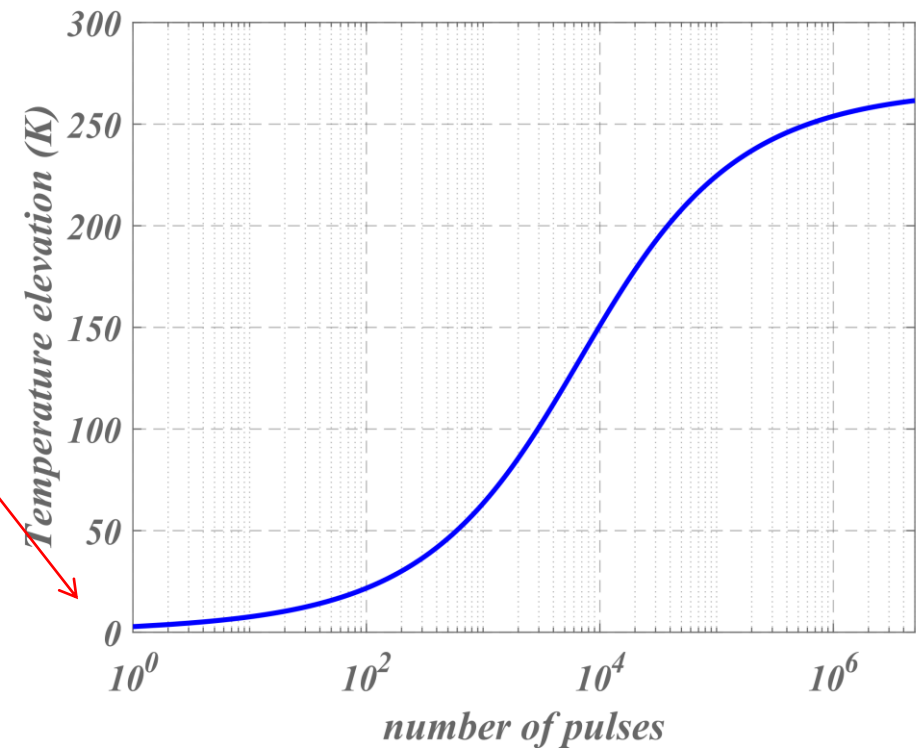
Ex : Pulse 1 ns @1MHz

$$n'' = 10^{-5}$$

1 pulse $\Rightarrow T_f = 3K$

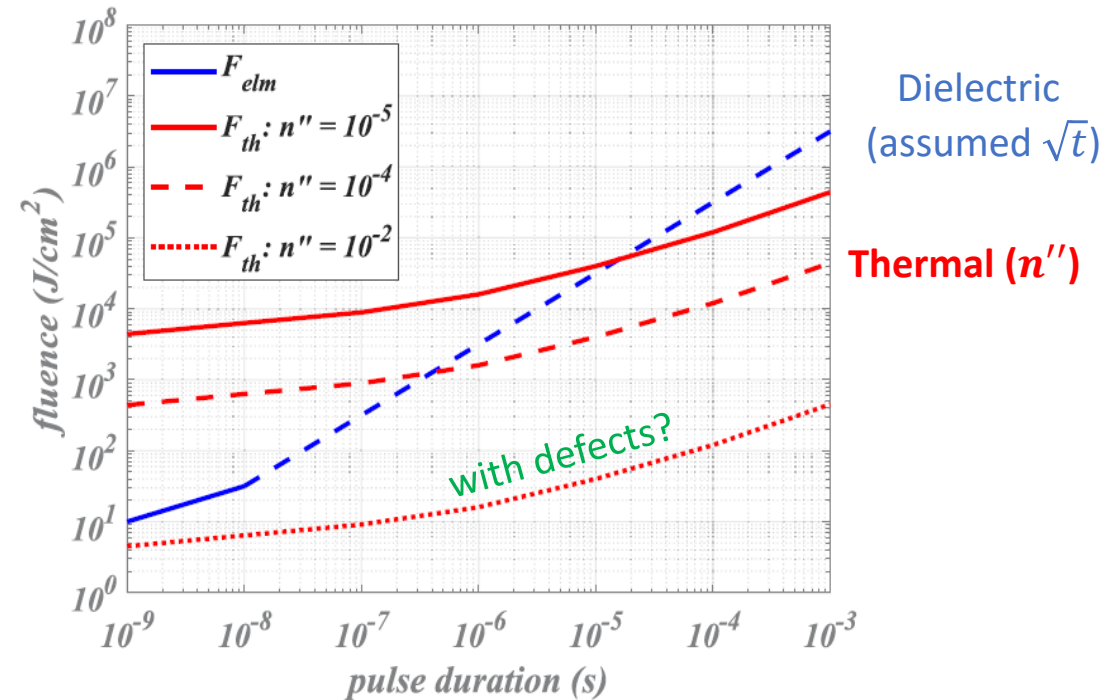


10^6 pulses (1s) $\Rightarrow T_f = 252K$



Thermal damage threshold

$$T(\text{pulse duration, energy, } n'') = T_f \Rightarrow \text{Thermal damage} \approx L(T_f, \text{pulse duration, } n'')$$

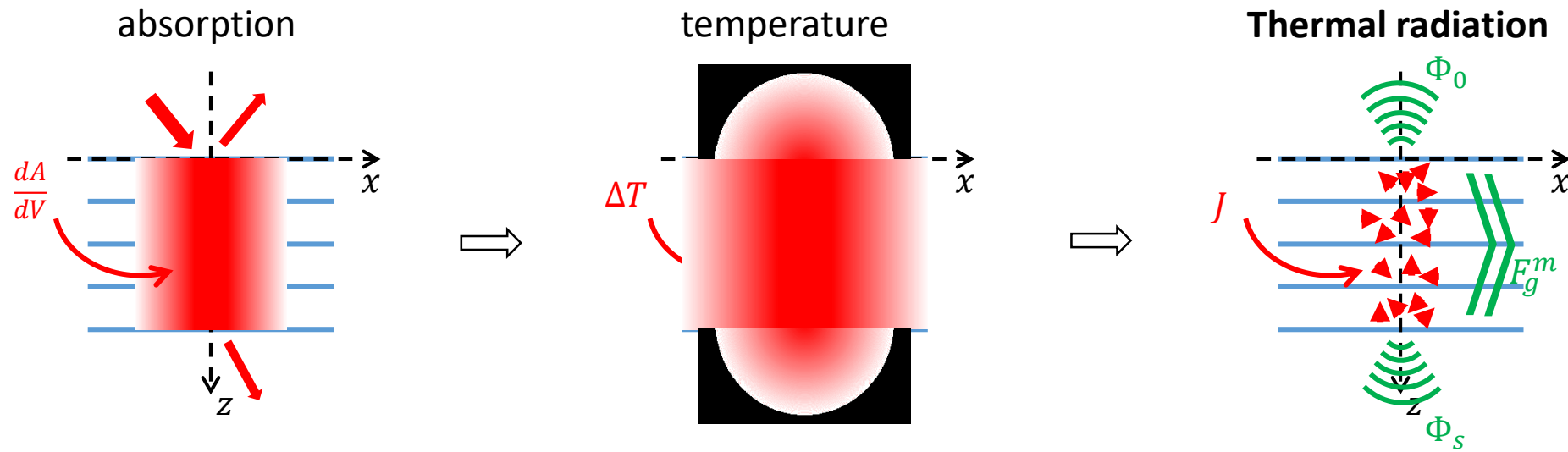


Thermal threshold is lower than the electromagnetic one, unless local defects intervene ($n'' > 10^{-2}$)

- R. M. Wood, *Laser-Induced Damage of Optical Materials*, Series in Optics and Optoelectronics (Institute of Physics, 2003)
- D. Ristau, *Laser-Induced Damage in Optical Materials* (CRC Press, 2015)
- P. Rouquette, C. Amra, M. Zerrad, C. Grèzes-Besset, and H. Krol, "Photo-induced temperature in optical interference coatings," *Opt. Express* 30, 46575-46601 (2022)

3- Rayonnement thermique photo-induit dans les filtres interférentiels

- S. M. Rytov, Yu. A. Kravtsov, and V. I. Tatarskii, *Principles of Statistical Radiophysics 3: Elements of Random Fields* (Springer-Verlag, 1989).
 - Z. M. Zhang, *Nano/Microscale Heat Transfer*, 2nd ed., Mechanical Engineering Series (Springer International Publishing, 2020).
- L. P. Wang, S. Basu, and Z. M. Zhang, "Direct and indirect methods for calculating thermal emission from layered structures with nonuniform temperatures," *J. Heat Transf.* **133**, (2011).
- M. Francoeur, M. Pinar Mengüç, and R. Vaillon, "Solution of near-field thermal radiation in one-dimensional layered media using dyadic Green's functions and the scattering matrix method," *J. Quant. Spectrosc. Radiat. Transf.* **110**, 2002–2018 (2009)
- J.-J. Greffet, R. Carminati, K. Joulain, J.-P. Mulet, S. Mainguy, and Y. Chen, "Coherent emission of light by thermal sources," *Nature* **416**, 61–64 (2002)



Maxwell equations

$$\text{rot} E = j\omega\mu H + \mathbf{M}[T(\vec{\rho}, \omega)] \quad \text{rot} H = -j\omega\epsilon E + \mathbf{J}[T(\vec{\rho}, \omega)]$$

How to get the currents « thermal currents » (M , J) ?

Fluctuation Dissipation Theorem (statistical physics)

$$\langle [x_0(t) - \bar{x}_0]^2 \rangle \ll 1 \Rightarrow x_0(t) \approx \bar{x}_0 \quad \left\{ \begin{array}{l} \mathcal{H}(x) = \mathcal{H}_0(x) - x f(t) \\ \langle x(t) \rangle = \bar{x}_0 + G *_t f \end{array} \right. \Rightarrow \left\{ \begin{array}{l} \langle |\check{x}(\omega)|^2 \rangle = \left(\frac{1}{\pi\omega} \right) \Theta(\omega, T) \text{Im}[\check{G}(\omega)] \\ \Theta(\omega, T) = \frac{\hbar\omega}{e^{\frac{\hbar\omega}{k_B T}} - 1} \end{array} \right.$$

Application to the matter polarizations

$$E \rightarrow \boxed{P_e = \varepsilon_0 \chi_e *_t E} \quad H \rightarrow \boxed{P_h = \chi_h *_t H}$$

$$\left\{ \begin{array}{l} \langle P_e(t, \vec{\rho}) \rangle = \varepsilon_0 \chi_e(t, \vec{\rho}) *_t E_0(t, \vec{\rho}) \\ \langle P_h(t, \vec{\rho}) \rangle = \chi_h(t, \vec{\rho}) *_t H_0(t, \vec{\rho}) \\ \delta W_e = -P_e \cdot E_0 \delta V \text{ and } \delta W_h = -\mu_0 P_h \cdot H_0 \delta V \end{array} \right. \Rightarrow \left\{ \begin{array}{l} \langle |\check{P}_e(\omega, \vec{\rho})|^2 \rangle \delta V = \left(\frac{1}{\pi\omega} \right) \Theta(\omega, T(\vec{\rho})) \text{Im}[\check{\epsilon}(\omega, \vec{\rho})] \\ \langle |\check{P}_h(\omega, \vec{\rho})|^2 \rangle \delta V = \frac{1}{\mu_0^2} \left(\frac{1}{\pi\omega} \right) \Theta(\omega, T(\vec{\rho})) \text{Im}[\check{\mu}(\omega, \vec{\rho})] \end{array} \right.$$

$$\theta(\omega, T) = \hbar \omega / (e^{\frac{\hbar\omega}{k_B T}} - 1)$$

The thermal currents are known

$$\theta(\omega, T) = \hbar \omega / (e^{\frac{\hbar \omega}{k_B T}} - 1)$$

$$\langle |\tilde{\mathbf{J}}(\omega)|^2 \rangle = \left(\frac{\omega}{\pi}\right) \theta(\omega, \mathbf{T}) \operatorname{Im}[\tilde{\boldsymbol{\epsilon}}(\omega)]$$

$$\langle |\tilde{\mathbf{M}}(\omega)|^2 \rangle = \left(\frac{\omega}{\pi}\right) \theta(\omega, \mathbf{T}) \operatorname{Im}[\tilde{\boldsymbol{\mu}}(\omega)]$$



Similar to a luminescent microcavity (Optics)

$$\operatorname{rot} \mathbf{E} = j\omega\mu\mathbf{H} + \mathbf{M}[T(\vec{\rho}, \omega)]$$

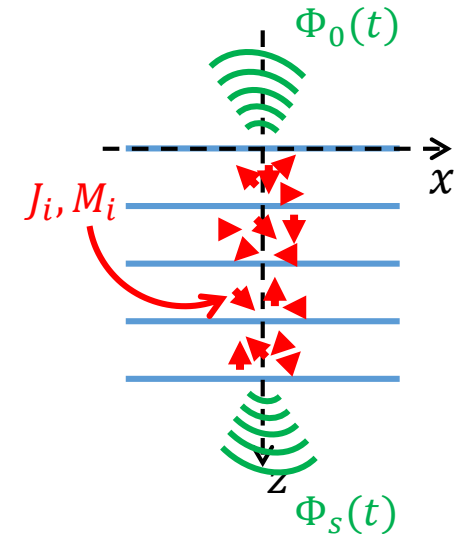
$$\operatorname{rot} \mathbf{H} = -j\omega\epsilon\mathbf{E} + \mathbf{J}[T(\vec{\rho}, \omega)]$$

- Each bulk is a source of thermal radiation
- All fields must be summed up: $\mathbf{E}_j = \sum_i^p \mathbf{E}_{ij}$



By reflection:
$$\frac{\partial \Phi_0}{\partial f \partial \vec{v} dS} = 2 \sum_{i=1}^p 4\pi f \tilde{\epsilon}_i'' \Re\{\tilde{n}_0\} |C'_{0,i-1}|^2 \frac{\beta_i^0(\nu, f)}{4|\tilde{n}_i|^2 |\Delta Y_{i-1}|^2} \Theta(2\pi f, T_i(\vec{r}, z_i))$$

By transmission:
$$\frac{\partial \Phi_s}{\partial f \partial \vec{v} dS} = 2 \sum_{i=1}^p 4\pi f \tilde{\epsilon}_i'' \Re\{\tilde{n}_s\} |C_{i,p}|^2 \frac{\beta_i^s(\nu, f)}{4|\tilde{n}_i|^2 |\Delta Y_i|^2} \Theta(2\pi f, T_i(\vec{r}, z_i))$$



Physical quantities: static versus photo-induced

Double flux density: $\frac{\partial \Phi}{\partial f \partial \vec{v}} = \sum_{i=1}^q L'_i(f, \nu) \left\{ \int_{\vec{r}} \Theta(2\pi f, T_i(\vec{r}, z_i)) d\vec{r} \right\}$ with $\theta(\omega, T) = \bar{h} \omega / (e^{\frac{\bar{h} \omega}{k_B T}} - 1)$



Per unit of wavelength and solid angle

$$\frac{\partial \Phi_u}{\partial \lambda \partial \Omega_u}$$



Angle-Resolved Thermal Radiation

(similar to angle-resolved scattering or $BRDF \cdot \cos \theta$)

$$\frac{\partial \Phi_u}{\Phi_0^+ \partial \lambda \partial \Omega_u}$$



Radiative spectral intensity

(normalization by the « thermal » surface)

$$\frac{\partial \Phi}{\partial \lambda \partial \Omega_u \partial S}$$



Emissivity

(normalization by black body radiation)

$$\epsilon_i(\lambda, \theta) = \frac{1}{I_b(\lambda, T_i)} \frac{\partial \Phi}{\partial \lambda \partial \Omega_u \partial S}$$

$$I_b(\lambda, T) = 2 \frac{k_0^2}{4\pi^2} \frac{c}{\lambda^2} \Theta\left(\frac{2\pi c}{\lambda}, T\right)$$

← Photo-induced T_p

Uniform T_p →

Blackbody radiation: $I_b(\lambda, T) = 2 \frac{k_0^2}{4\pi^2} \frac{c}{\lambda^2} \Theta\left(\frac{2\pi c}{\lambda}, \mathbf{T}\right)$ ← unique Tp

Coating radiation: $\frac{\partial \Phi}{\partial f \partial \vec{v}} = \sum_{i=1}^q L'_i(f, \nu) \left\{ \int_{\vec{r}} \Theta(2\pi f, \mathbf{T}_i(\vec{r}, \mathbf{z}_i)) d\vec{r} \right\}$ ← Tp distribution

\Rightarrow Emissivity depends on both optical and thermal parameters

$$\boldsymbol{\varepsilon}_i(\lambda, \boldsymbol{\theta}) \neq \mathbf{A}_i(\lambda, \boldsymbol{\theta}) \text{ (short pulse regime)}$$

Case of uniform temperature

$$\frac{\partial \Phi}{\partial f \partial \vec{v}} = \sum_{i=1}^q L'_i(f, \nu) \left\{ \int_{\vec{r}} \Theta(2\pi f, T_i(\vec{r}, \mathbf{z}_i)) d\vec{r} \right\} \approx \left\{ \int_{\vec{r}} \Theta(2\pi f, T) d\vec{r} \right\} \sum_{i=1}^q L'_i(f, \nu)$$

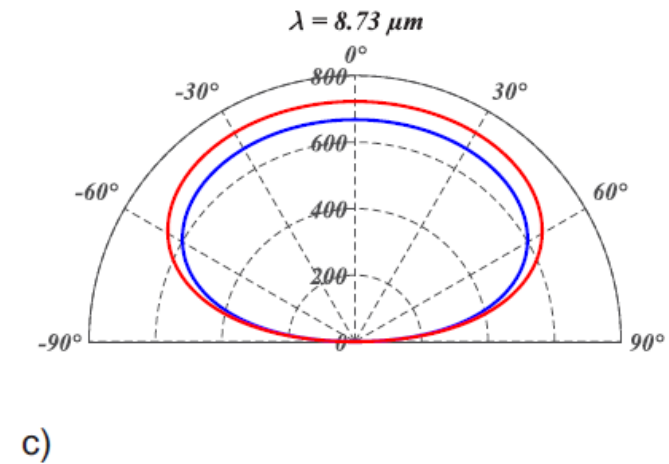
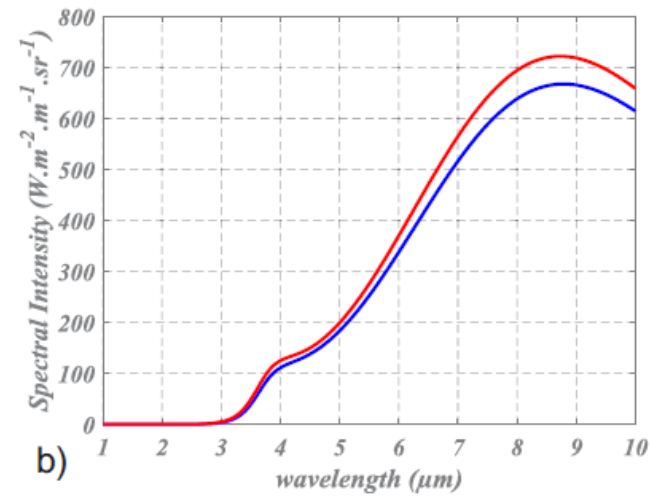
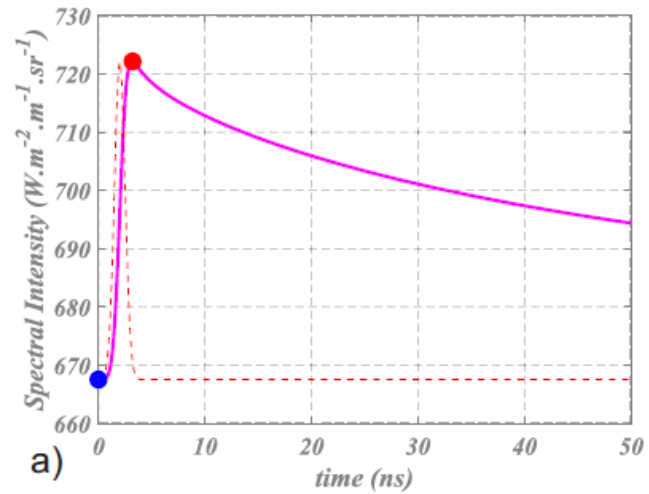
Emissivity identifies to absorption:

$$\boldsymbol{\varepsilon}_i(\lambda, \boldsymbol{\theta}) = \mathbf{A}_i(\lambda, \boldsymbol{\theta}) \text{ (long pulse regime)}$$

Not the case for the ns regime, not suitable for the trapped light

Variation versus time, wavelength and direction

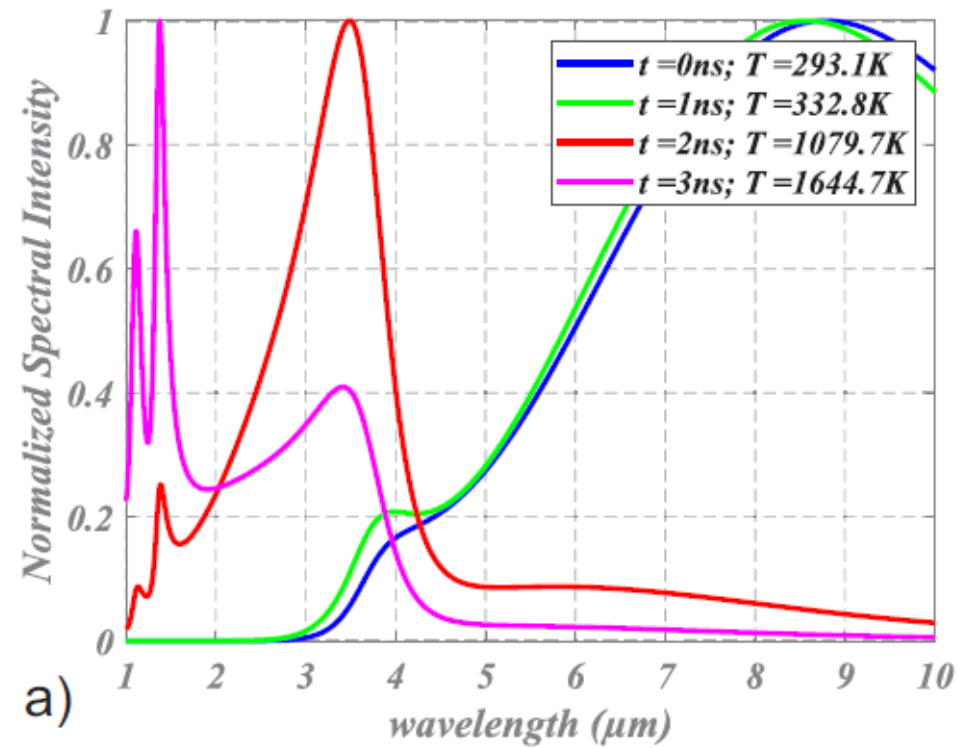
QW@ $2\mu\text{m}$, $L = B_a F_2$, $H = G_e$,
 on G_e substrate, $n'' = 10^{-4}$
 1mJ , 1ns , $i = 0^\circ$



Slight temperature increase \Leftrightarrow slight modification of blackbody radiation

Variation with incident energy (or temperature)

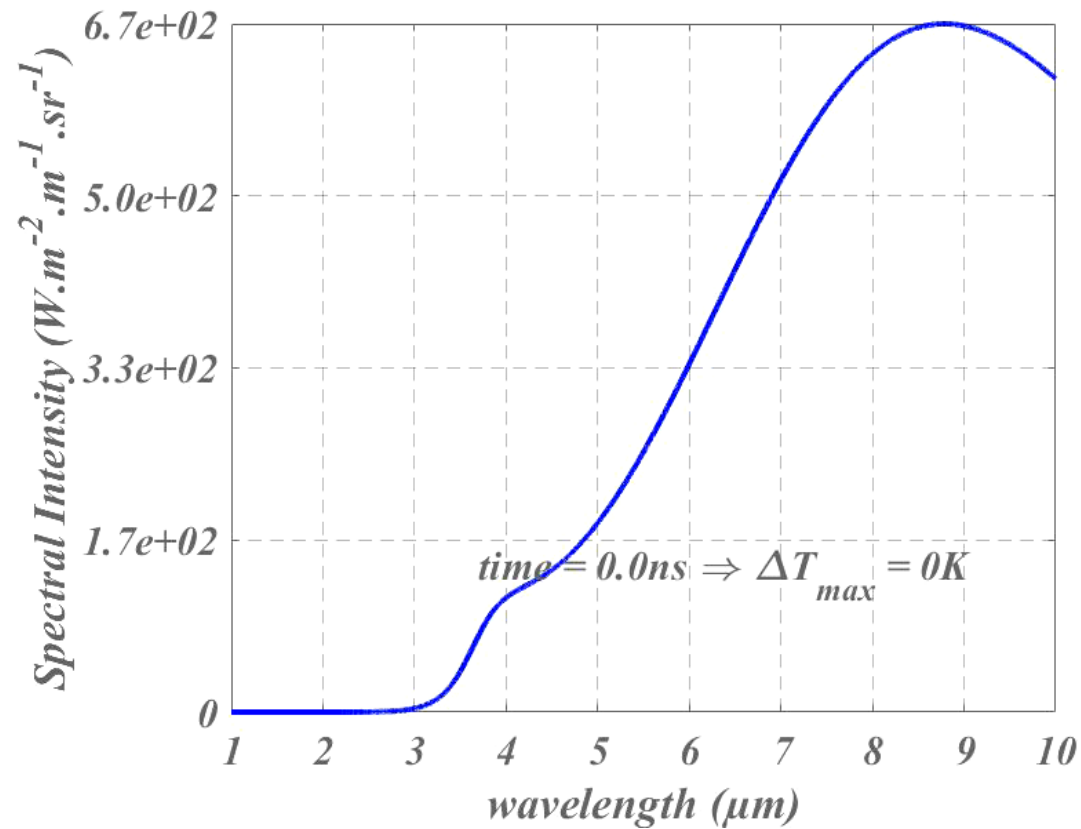
(damage non considered)



At short wavelengths,
the coating filters its own radiation

Blackbody modification at short wavelengths = interaction with the multilayer

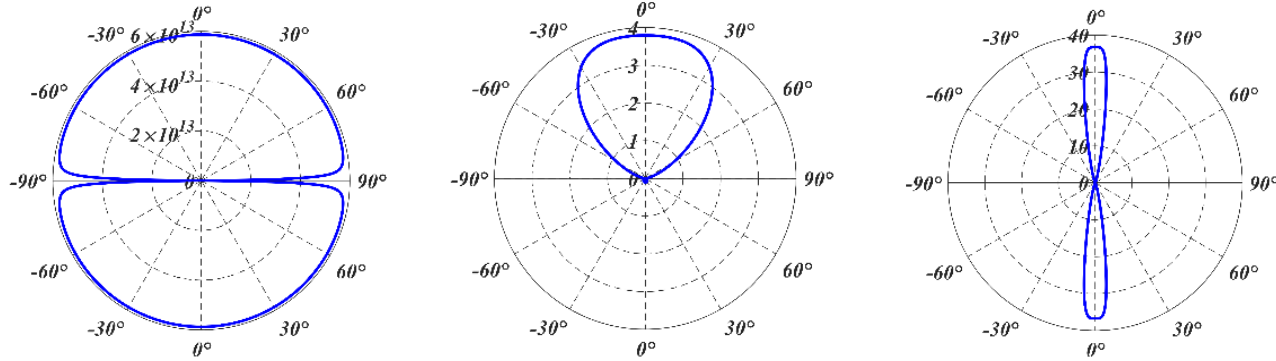
Real-time illustration



QW@ $2\mu\text{m}$, $L = B_a F_2$, $H = G_e$,
on G_e substrate, $n'' = 10^{-4}$
 1mJ , 1ns , $i = 0^\circ$

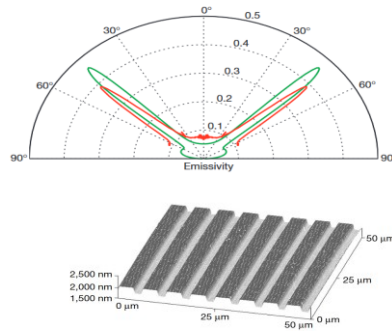
P. Rouquette, C. Amra, M. Zerrad, C. Grèzes-Besset, and H. Krol, "Photo-induced thermal radiation of optical interference coatings submitted to a spatio-temporal illumination," *Opt. Express* **31**, 35431-35452 (2023)

Shaping thermal radiation with multilayers?

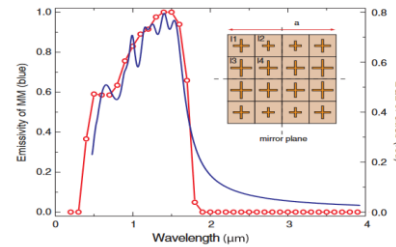


C. Amra, M. Lequime, M. Zerrad, «*Electromagnetic Optics of Thin Film Coatings : Light Scattering, Giant Field Enhancement, and Planar Microcavities* », Cambridge University Press, 2020, 9781108772372

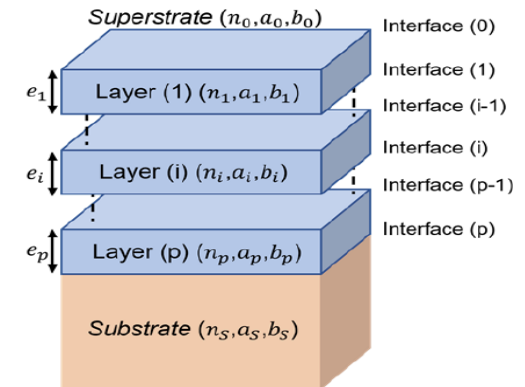
Gratings and metasurfaces were already used to produce **narrow-band emissivity enhancement**



J.-J. Greffet, R. Carminati, K. Joulain, J.-P. Mulet, S. Mainguy, and Y. Chen, "Coherent emission of light by thermal sources," *Nature* **416**, 61–64 (2002).

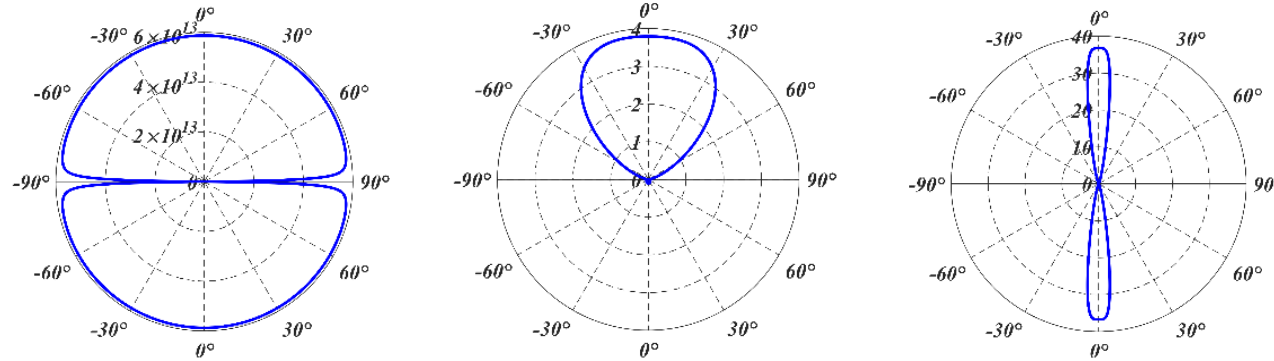


X. Liu, T. Tyler, T. Starr, A. F. Starr, N. M. Jokerst, and W. J. Padilla, "Taming the Blackbody with Infrared Metamaterials as Selective Thermal Emitters," *Phys. Rev. Lett.* **107**, 045901 (2011).



Multidielectrics are known to offer a large number of degrees of freedom

Retour aux techniques de microcavités luminescentes



$$\frac{\partial \Phi_0}{\partial f \partial \vec{v} dS} = 2 \sum_{i=1}^p 4\pi f \tilde{\epsilon}_i'' \Re\{\tilde{n}_0\} |C'_{0,i-1}|^2 \frac{\beta_i^0(\nu, f)}{4|\tilde{n}_i|^2 |\Delta Y_{i-1}|^2} \Theta(2\pi f, T_i(\vec{r}, z_i))$$

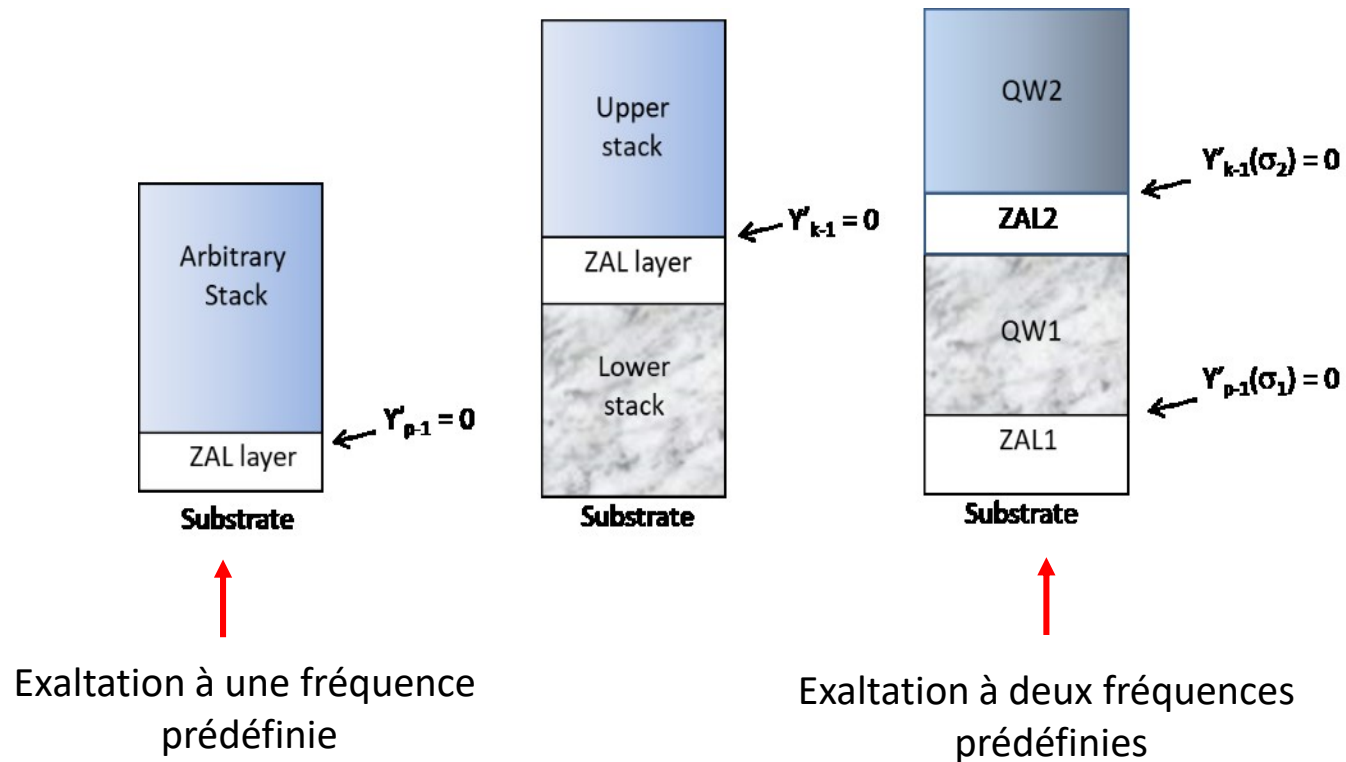
$$\frac{\partial \Phi_s}{\partial f \partial \vec{v} dS} = 2 \sum_{i=1}^p 4\pi f \tilde{\epsilon}_i'' \Re\{\tilde{n}_s\} |C_{i,p}|^2 \frac{\beta_i^s(\nu, f)}{4|\tilde{n}_i|^2 |\Delta Y_i|^2} \Theta(2\pi f, T_i(\vec{r}, z_i))$$

La différence d'admittance ΔY_i est le paramètre clé qui régit les exaltations/inhibitions

Recherche d'une exaltation « géante » de l'émissivité

$$\text{Exaltation à la fréquence } \nu_m \Leftrightarrow \Delta Y(\nu_m) = 0$$

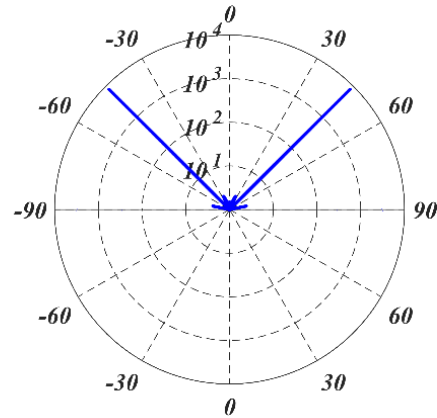
Pas de solution en espace libre \Rightarrow régime TIR dans un milieu \Rightarrow couche d'admittance nulle (ZAL)



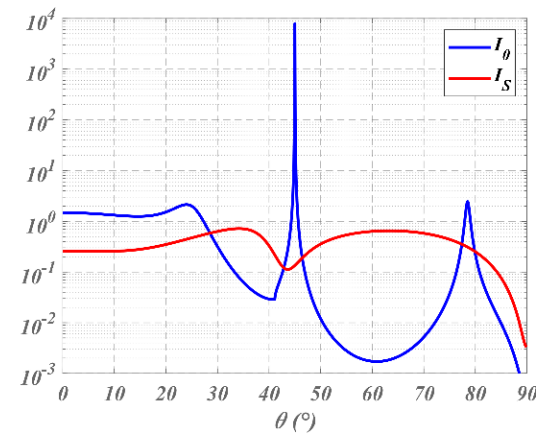
Résultats numériques avec des structures ZAL

Exaltations de plusieurs décades à une fréquence et polarisation imposées

TE, 45°, 633nm



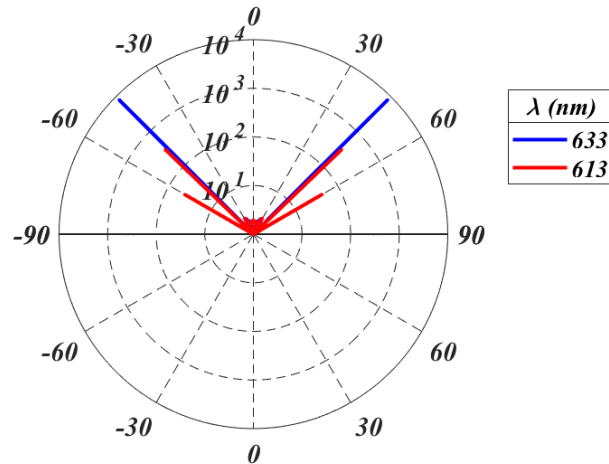
TE, 45°, 633nm



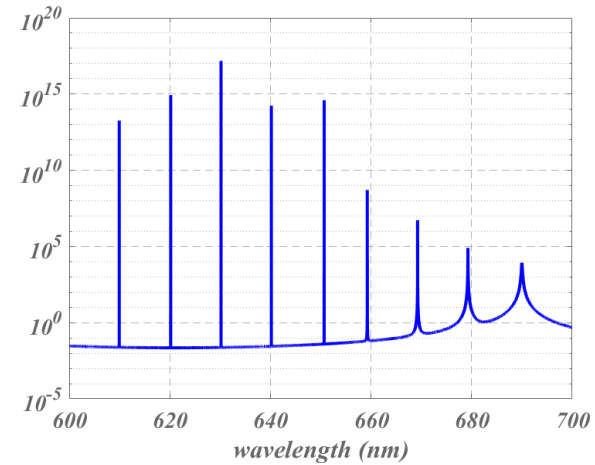
À des angles différents

633nm, 45°

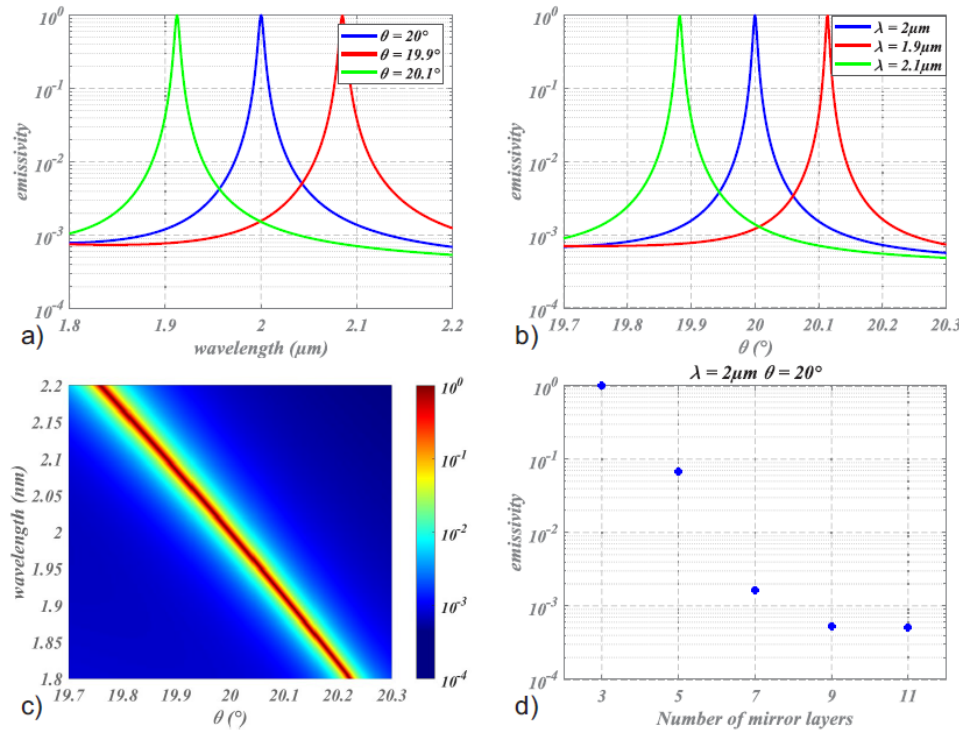
613nm, 35°



À plusieurs longueurs d'onde



Application au rayonnement thermique

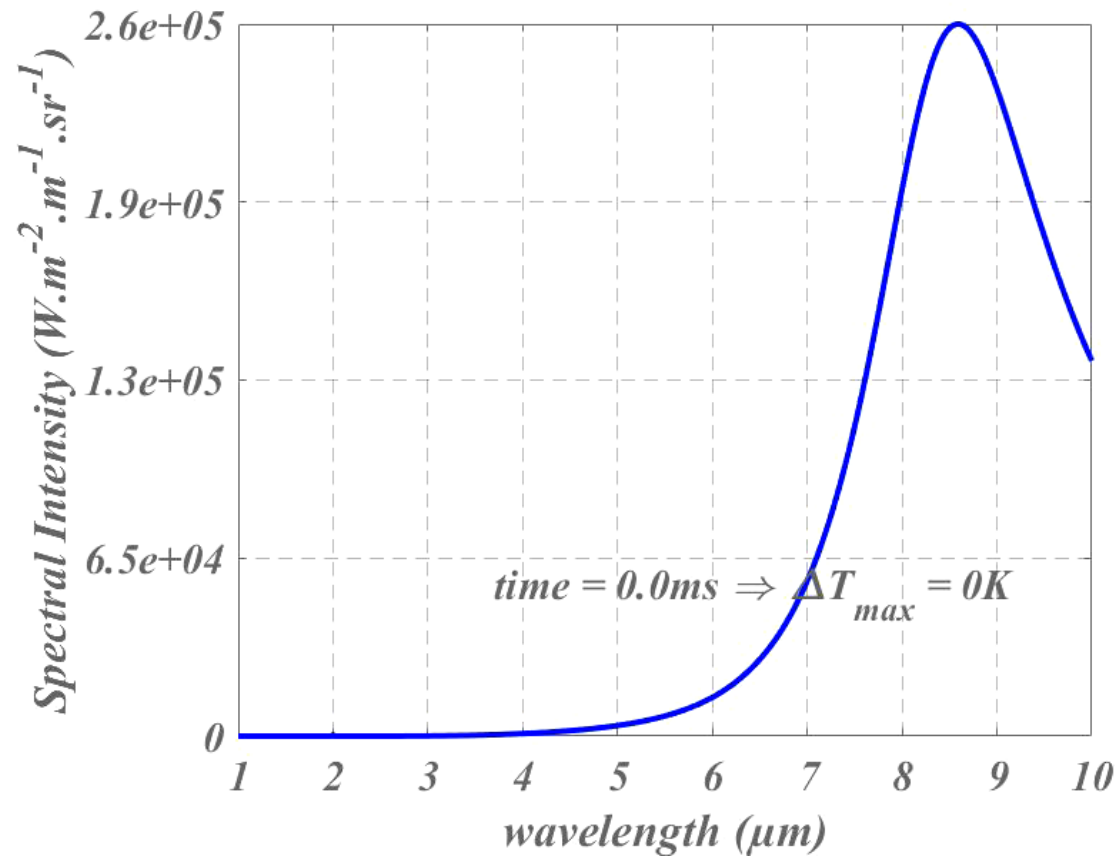


*Miroir multidiélectrique@2 μm ,
direction 20 $^\circ$, polarisation TE, $n'' = 10^{-4}$*

$$\theta = f(\lambda)$$

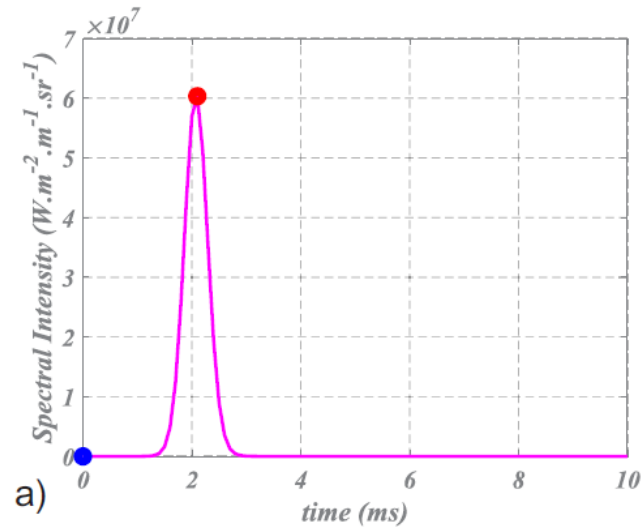
Malgré un indice imaginaire de 10^{-4} , on peut imposer une « **émissivité bande étroite proche de 1** »
dans des fenêtres spectrales ou angulaires **prédéfinies**

Real-time illustration

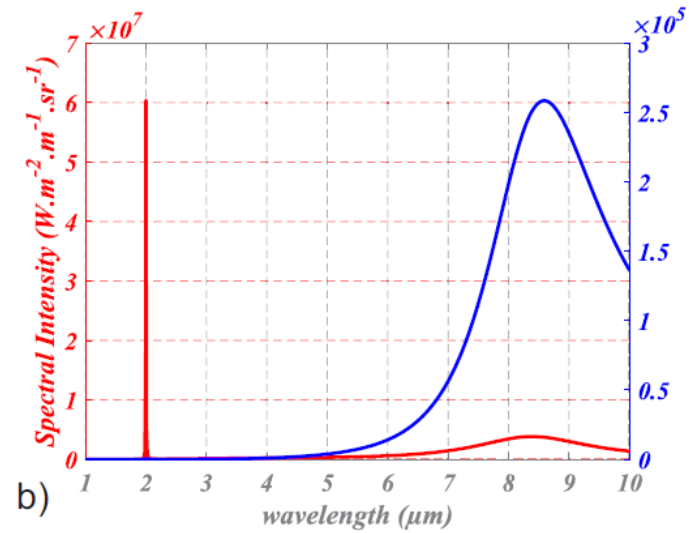


QW@2 μm , $L = B_a F_2$, $H = G_e$,
on G_e substrate, $n'' = 10^{-4}$
1mJ, 1ms, 20°, TE

ThR @2 μm , direction 20°

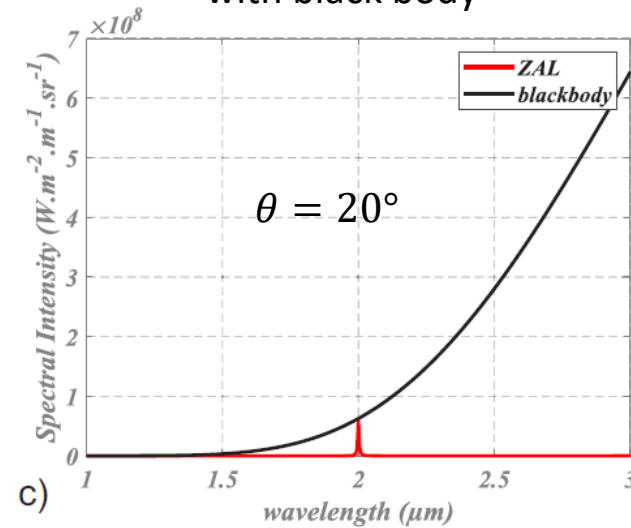


ThR at different times



Blue: 0K (0ms)
Red: 250K (2ms)

Comparison
with black body

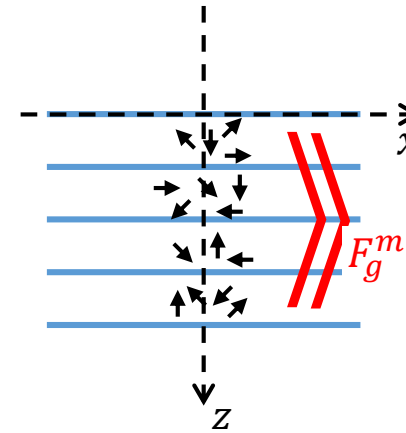
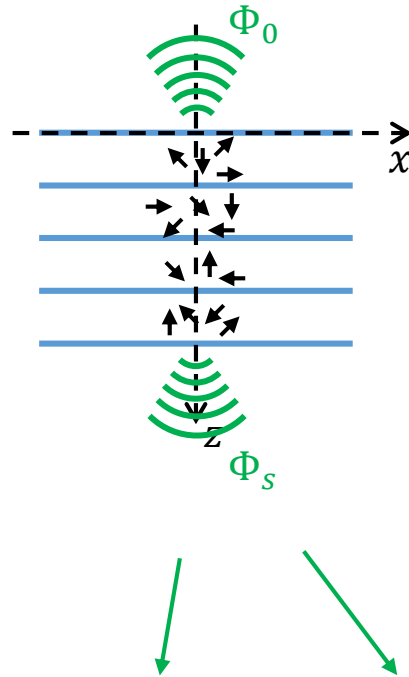


Conclusion partielle

- Pour l'instant: un effort limité pour la conception/réalisation d'étalons
- Ok en régime statique
- Puissance moindre avec des empilements métal/diélectrique
- Contrôle de T_p

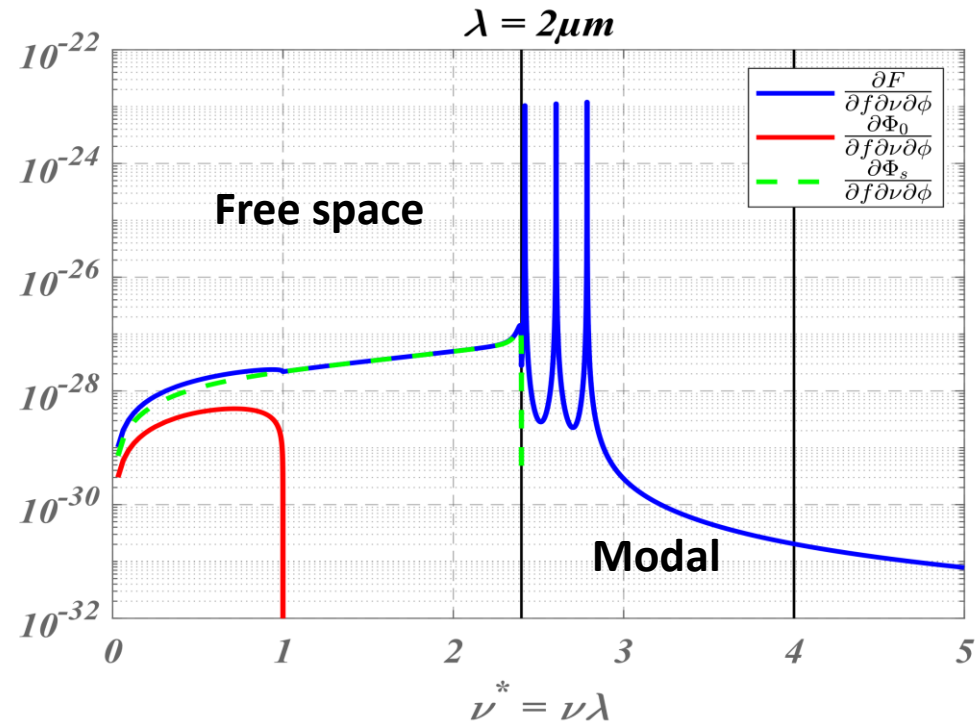
4- Le rayonnement thermique piégé

ThR trapped in the form of guided modes in multilayers



How much ThR in this range?





Trapped ThR is higher by a factor 10

Merci!

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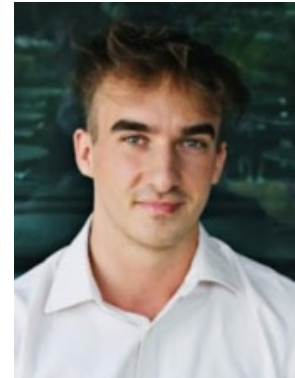
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